Homework3

(All questions carry 10 marks each)

Exercise Set 3.1, #12, page 106

x=16, y=4

 $\sqrt{x} = 4$; $\sqrt{y} = 2$; $\sqrt{x} + \sqrt{y} = 6$

 $\sqrt{(x+y)} = \sqrt{20} = 4.47$

Exercise Set 3.1, #16bdf, page 107

- b). \forall real number x, x is positive, negative or zero.
- d). \forall logician x, x is not lazy.
- f). \forall real number x, square of x is not equal to -1.

Exercise Set 3.1, #32bd, page 108

- b). True. Any number greater than 2 will have a square greater than 4.
- d). True. $x^2>4 -> x>2$ or x<-2 but |x|>2.

Exercise Set 3.2, #2, page 116

- c). Some dogs are disloyal.
- f). There is a dog that is disloyal

Exercise Set 3.2, #17, page 116

 \exists an integer d such that 6/d is an integer and d \neq 3.

Exercise Set 3.2, #44, page 117

It is not the case that if a person is happy then the person is having a large income. In other words there is a person who is happy and does not have a large income.

Exercise Set 3.3, #10, page 129

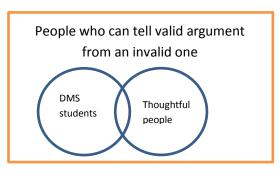
- a). There is at least one desert chosen by every student. True.
- b). There is a salad chosen by every student. False-> Yuen did not choose a salad.
- c). There exists a particular desert such that all students chose that desert. True.
- d). There exists a particular beverage such that all students chose that beverage. False.
- e). There is a particular item such that none of the students chose that item. False.
- f). There is a station such that chose atleast one item from that station. True->Beverage

Exercise Set 3.3, #41cdfgh, page 130

- c). True: When you add 1 to any real number we again get a real number.
- d). True: Number multiplied by its reciprocal is 1.
- f). False: Consider x=1 and y=3. Hence, z=-2 (which is not in Z+).
- g). True: Consider x=1 and y=3. Hence, z= -2 (which is in Z).
- h). True: let u=1/2, v=8, uv=4 < v

Exercise Set 3.4, #22, page 143

The argument is invalid



Exercise Set 3.4, #26, page 143

The argument is valid

