## CMSC 442/653 Fall 2007

**Instructor: Dr. Lomonaco** 

## Homework 1

- **Listening Assignment:** Listen to Beethoven's 5-th symphony.
- Reading Assignment: http://www.cs.umbc.edu/~lomonaco/s06/652/slides/Equilateral-Triangle.pdf
- Optional Reading assignment: Peterson & Weldon, "Error-Correcting Codes," MIT Press, (Second Edition), Chapter 2.
- 1) Construct the multiplication table of the group of symmetries of the equilateral triangle given by the presentation

$$(\rho, \sigma : \rho^3 = 1, \sigma^2 = 1, \rho\sigma = \sigma\rho^2)$$

Assume that the distinct group elements are:

$$1, \rho, \rho^2, \sigma, \rho\sigma, \rho^2\sigma$$

2) Construct the multiplication table of the group of symmetries of the square given by the presentation

$$(\rho, \sigma : \rho^4 = 1, \sigma^2 = 1, \rho \sigma = \sigma \rho^3)$$

Assume that the distinct group elements are:

$$\left\{ \rho^m \sigma^n : 0 \le m < 4, 0 \le n < 2 \right\}$$

## Additional problem for grad students in CMSC 653:

- **Grad3**) Let S be a set with an associative binary operation  $\bullet: S \times S \to S$ . Let  $e_L$  be a left identity of S (i.e.,  $e_L \bullet s = s \ \forall s \in S$ ), and let  $e_R$  be a right identity of S (i.e.,  $s \bullet e_R = s \ \forall s \in S$ ).
  - a) Prove that  $e_L = e_R$ .
  - b) Also prove that **S** can have at most one 2-sided identity.
- **Grad4)** Let S be a set with an associative binary operation  $\bullet: S \times S \to S$  and a 2-sided identity e, and let  $s \in S$ . Let  $\widetilde{s_L}$  and  $\widetilde{s_R}$  be elements of S such that

$$\widetilde{s_L} \bullet s = e = s \bullet \widetilde{s_R}$$

Prove that  $\widetilde{s_L} = \widetilde{s_R}$ .