



*Lisp*



## *Versions of LISP*

- **Lisp** is an old language with many variants
- Lisp is alive and well today
- Most modern versions are based on **Common Lisp**
- **LispWorks** is based on Common Lisp
- **Scheme** is one of the major variants
- The essentials haven't changed much

## *Recursion*

- Recursion is essential in Lisp
- A *recursive definition* is a definition in which
  - certain things are specified as belonging to the category being defined, and
  - a rule or rules are given for building new things in the category from other things already known to be in the category.

## *Informal Syntax*

- An *atom* is either an integer or an identifier.
- A *list* is a left parenthesis, followed by zero or more S-expressions, followed by a right parenthesis.
- An *S-expression* is an atom or a list.
- Example: (A (B 3) (C) ( ( ) ) )

## *Formal Syntax (approximate)*

- $\langle \text{S-expression} \rangle ::= \langle \text{atom} \rangle \mid \langle \text{list} \rangle$
- $\langle \text{atom} \rangle ::= \langle \text{number} \rangle \mid \langle \text{identifier} \rangle$
- $\langle \text{list} \rangle ::= ( \langle \text{S-expressions} \rangle )$
- $\langle \text{S-expressions} \rangle ::= \langle \text{empty} \rangle$   
|  $\langle \text{S-expressions} \rangle \langle \text{S-expression} \rangle$
- $\langle \text{number} \rangle ::= \langle \text{digit} \rangle \mid \langle \text{number} \rangle \langle \text{digit} \rangle$
- $\langle \text{identifier} \rangle ::= \text{string of printable characters, not including parentheses}$

## *T and NIL*

- NIL is the name of the empty list
- As a test, NIL means “false”
- T is usually used to mean “true,” but...
- ...anything that isn't NIL is “true”
- NIL is both an atom and a list
  - it's defined this way, so just accept it

## *Function calls and data*

- A function call is written as a list
  - the first element is the name of the function
  - remaining elements are the arguments
- Example: (F A B)
  - calls function F with arguments A and B
- Data is written as atoms or lists
- Example: (F A B) is a list of three elements
  - Do you see a problem here?

## *Quoting*

- Is (F A B) a call to F, or is it just data?
- All *literal data* must be quoted (atoms, too)
- (QUOTE (F A B)) is the list (F A B)
  - QUOTE is a “special form”
  - The arguments to a special form are not evaluated
- '(F A B) is another way to quote data
  - There is just one single quote at the beginning
  - It quotes one S-expression

## *Basic Functions*

- CAR returns the head of a list
- CDR returns the tail of a list
- CONS inserts a new head into a list
- EQ compares two atoms for equality
- ATOM tests if its argument is an atom

## *Other useful Functions*

- (NULL S) tests if S is the empty list
- (LISTP S) tests if S is a list
- LIST makes a list of its (evaluated) arguments
  - (LIST 'A '(B C) 'D) returns (A (B C) D)
  - (LIST (CDR '(A B)) 'C) returns ((B) C)
- APPEND concatenates two lists
  - (APPEND '(A B) '((X) Y) ) returns (A B (X) Y)

## CAR

- The CAR of a list is the first thing in the list
- CAR is only defined for *nonempty* lists

If L is

Then (CAR L) is

(A B C)

A

((X Y) Z)

(X Y)

(( ) ( ))

( )

( )

*undefined*

## CDR

- The CDR of a list is what's left when you remove the CAR
- CDR is only defined for *nonempty* lists
- The CDR of a list is always a list


## CDR examples

<u>If L is</u>	<u>Then (CDR L) is</u>
(A B C)	(B C)
((X Y) Z)	(Z)
(X)	()
((())())	((()))
()	<i>undefined</i>

## CONS

- CONS takes two arguments
  - The first argument can be any S-expression
  - The second argument should be a list
- The result is a new list whose CAR is the first argument and whose CDR is the second
- Just move one parenthesis to get the result:

CONS of A (B C) gives (A B C)



## CONS examples

- CONS puts together what CAR and CDR take apart

<u>L</u>	<u>(CAR L)</u>	<u>(CDR L)</u>	<u>(CONS (CAR L) (CDR L))</u>
(A B C)	A	(B C)	(A B C)
((X Y) Z)	(X Y)	(Z)	((X Y) Z)
(X)	X	()	(X)
(( ) ())	()	(( ))	(( ) ())
()	<i>undefined</i>	<i>undefined</i>	<i>undefined</i>

## Dotted Pairs

- The second argument to CONS should be a list
- If it isn't, you get a *dotted pair*
- CONS of A and B is (A . B)
- We aren't using dotted pairs in this class
- If you get a dotted pair, it's because you gave CONS an atom as a second argument



## *EQ*

- EQ tests whether two atoms are equal
  - Integers are a kind of atom
- EQ is undefined for lists
  - it might work for lists, it might not
  - but it won't give you an error message
- As with any predicate, EQ returns either NIL or something that isn't NIL

## *ATOM*

- ATOM takes any S-expression as an argument
- ATOM returns "true" if the argument you gave it is an atom
- As with any predicate, ATOM returns either NIL or something that isn't NIL

## COND

- COND implements the if...then...elseif...then...elseif...then... control structure
- The arguments to a function are evaluated before the function is called
  - This isn't what you want for COND
- COND is a *special form*, not a function

## Special forms

- A *special form* is like a function, but it evaluates the arguments as it needs them
- COND, QUOTE and DEFUN are special forms
- You can define your own special forms
- We won't be defining special forms in this course

## *Form of the COND*

```
(COND
  (condition1 result1)
  (condition2 result2)
  ...
  (T resultN) )
```

## *Defining Functions*

- (DEFUN *function\_name* *parameter\_list* *function\_body*)
- Example: Test if the argument is the empty list
- (DEFUN **NULL** **(X)**  
 (COND  
 (X NIL)  
 (T T) ) )

## *Example: MEMBER*

- As an example we define MEMBER, which tests whether an atom is in a list of atoms
- (DEFUN MEMBER (A LAT)  
 (COND  
 ((NULL LAT) NIL)  
 ((EQ A (CAR LAT)) T)  
 (T (MEMBER A (CDR LAT))) ) )
- MEMBER is typically a built-in function

## *Rules for Recursion*

- Handle the base (“simplest”) cases first
- Recur only with a “simpler” case
  - “Simpler” = more like the base case
- Don’t alter global variables (you can’t anyway with the Lisp functions I’ve told you about)
- Don’t look down into the recursion

## *Guidelines for Lisp Functions*

- Unless the function is trivial, start with COND.
- Handle the base case first.
- Avoid having more than one base case.
- The base case is usually testing for NULL.
- Do something with the CAR and recur with the CDR.

## *Example: UNION*

```
(DEFUN UNION (SET1 SET2)
  (COND
    ((NULL SET1) SET2)
    ((MEMBER (CAR SET1) SET2)
     (UNION (CDR SET1) SET2) )
    (T (CONS (CAR SET1)
              (UNION (CDR SET1) SET2) )) ) )
```

## *Still more useful Functions*

- (LENGTH L) returns the length of list L
- (RANDOM N) , where N is an integer, returns a random integer  $\geq 0$  and  $< N$ .

*The End*