
Binary Search Tree
A Binary Search Tree is a Binary Tree in which, at every
node v , the values stored in the left subtree of v are less
than the value at v and the values stored in the right subtree
are greater.
The elements in the BST must be comparable.
Duplicates are not allowed in our discussion.
Note that each subtree of a BST is also a BST.

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A BST of integers

Describe the values which might appear in the subtrees
labeled A, B, C, and D
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BST Implementation
stores


- It is dynamic.
- The elements are ordered in the following ways
- inorder -- as dictated by operator<
- preorder, postorder, levelorder -- as
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BST Implementation template <typename Comparable>
class BinarySearchTree
$\{$
const Comparable \& findMin( ) const;
const Comparable \& findMax ( ) const;
bool contains ( const Comparable \& x ) const;
bool isEmpty ( ) const;
void printTree ( ) const;
void makeEmpty ( ) ;
void insert (const Comparable \& x )i
void remove( const Comparable \& x )i
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BST Implementation (2)
const BinarySearchTree \&
operator=( const BinarySearchTree \& rhs );
private:
struct BinaryNode
\{
Comparable element;
BinaryNode *left;
BinaryNode *right;


$$
\begin{aligned}
& \ddot{u} \\
& u \\
& \vdots \\
& 0 \\
& 0 \\
& u
\end{aligned}
$$

$$
\therefore
$$

BST Implementation (3)

$$
\begin{gathered}
\text { // private data } \\
\text { BinaryNode *ro }
\end{gathered}
$$

$$
\begin{aligned}
& \text { BST }{ }^{66} \text { contains }{ }^{99} \text { method } \\
& \text { // Returns true if } x \text { is found (contained) in the } \\
& \text { bool contains ( const comparable \& } x \text { ) const } \\
& \left\{\begin{array}{l}
\text { \{eturn contains }(x, \text { root }) ;
\end{array}\right. \\
& \text { \} rement }
\end{aligned}
$$



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$10$
Successor of a node v in a BST is the node that holds the data
value that immediately follows the data at v in order.
Finding Successor
-v has right subtree
• successor is smallest value in right subtree
(the leftmost node in the right subtree)
-v does not have right subtree

• | successor is first node on path back to root that does not have v |
| :--- |
| in its right subtree |




The insert Operation

$$
\begin{aligned}
& \text { // Internal method to insert into a subtree. } \\
& \text { // } x \text { is the item to insert. } \\
& \text { // } x \text { is the node that roots the subtree. } \\
& \text { // Set the new root of the subtree. }
\end{aligned}
$$

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Implementation of makeEmpty




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Tree Iterators As we know there are several ways to traverse through
a BST. For the user to do so, we must supply
different kind of iterators. The iterator type defines
how the elements are traversed.

- InOrderIterator<T> *InOrderBegin ( );
- PerOrderIterator<T> *PreOrderBegin ( );
- PostOrderIterator<T> *PostOrderBegin ( );
- LevelOrderIterator<T> *LevelOrderBegin ( );
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\}
InOrder Tree Iterator Implementation
Approach 1: Store traversal in list (private data
member). Return iterator for list. template <typename $\mathrm{T}>$
InOrderIterator<T> BinaryTree: :InorderBegin ( )
$\{$
$\quad$ m_theList $=$ new List<T>;
$\quad$ FillListInorder (m_theList, getRoot ( ) $;$
$\quad$ return m_theList->GetIterator ()$;$

$$
\begin{aligned}
& \text { InOrder Tree Iterator Implemenation (2) } \\
& \text { Approach 2: store traversal in stack to mimic recursive traversal } \\
& \text { template <typename } T> \\
& \text { class InorderIterator } \\
& \{ \\
& \text { private: } \\
& \text { Stack<* BinaryNode<T\gg m_stack; } \\
& \text { public: } \\
& \text { InorderIterator (BinaryNode<T> *t); }
\end{aligned}
$$

InOrder Tree Iterator Implementation (4)

return top->element;

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