#### CMSC 341

#### Binary Search Trees

### Binary Search Tree

node v, the value stored in the left child node is less than A Binary Search Tree is a Binary Tree in which, at every the value at v and the value stored in the right child is greater.

The elements in the BST must be comparable.

Duplicates are not allowed.

### **BST** Implementation

#### The SearchTree ADT

- A search tree is a binary search tree which stores homogeneous elements with no duplicates.
- It is dynamic.
- The elements are ordered in the following ways
- inorder -- as dictated by operator
- preorder, postorder, levelorder -- as dictated by the structure of the tree
- element of the tree. ITEM NOT FOUND is provided [TEM NOT FOUND, that is guaranteed to not be an Each BST maintains a simple object, known as to the constructor. (author's code)

### BinarySearchTree class

const; rhs); BinarySearchTree (const Comparable& notFnd); const Comparable& find(const Comparable& x) BinarySearchTree& rhs); BinarySearchTree (const BinarySearchTree& const BinarySearchTree &operator=(const void insert (const Comparable& x); void remove (const Comparable& x); const Comparable& findMin() const; const Comparable& findMax() const; template <class Comparable> void printTree() const; class BinarySearchTree { bool isEmpty() const; ~BinarySearchTree(); void makeEmpty(); public:

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BinarySearchTree class (cont)		BinaryNode <comparable> *root;</comparable>	const Comparable ITEM_NOT_FOUND;	<pre>const Comparable&amp; elementAt(BinaryNode<comparable> *t) const;</comparable></pre>	void insert (const Comparable& x,	BinaryNode <comparable> *&amp; t) const;</comparable>	void remove (const Comparable& א, BinaryNode <comparable> אג נ) const;</comparable>	<pre>BinaryNode<comparable>* findMin(BinaryNode<comparable>* t const;</comparable></comparable></pre>	<pre>BinaryNode<comparable>* findMax(BinaryNode<comparable>* t)const;</comparable></comparable></pre>	BinaryNode <comparable>*</comparable>	<pre>find(const Comparable&amp; x, BinaryNode<comparable>* t) const;</comparable></pre>	void makeEmpty(BinaryNode <comparable> *&amp; t) const;</comparable>	void printTree(BinaryNode <comparable* const;<="" t)="" th=""><th><pre>BinaryNode<comparable>* clone(BinaryNode<comparable>* t)const;</comparable></comparable></pre></th><th></th></comparable*>	<pre>BinaryNode<comparable>* clone(BinaryNode<comparable>* t)const;</comparable></comparable></pre>	
	private:	BinaryNc	const Cc	const Cc ele	void ins	Bin	void ren Bin	BinaryNc fin	BinaryNc fin	BinaryNc	fin	void mak	void pri	BinaryNc	: {

## **BinarySearchTree Implementation**

••• const Comparable &BinarySearchTree<Comparable> return elementAt(find (x, root)); find(const Comparable& x) const { template <class Comparable>

return t == NULL ? ITEM\_NOT\_FOUND : t->element; const Comparable& BinarySearchTree<Comparable> elementAt(BinaryNode<Comparable>\* t) const template <class Comparable>

find(const Comparable& x, BinaryNode<Comparable>\* t) const return find(x, t->right); BinaryNode<Comparable>\* BinarySearchTree<Comparable> else if (x < t->element) return find(x, t->left); if (t == NULL) return NULL; if (t->element < x) template <class Comparable> else

return t; // Match

else

# Asymptotic performance is O(height) in all cases

3/15/2005

## Performance of find

Searching in randomly built BST is O(lg n) on average

- but generally, a BST is not randomly built

### Predecessor in BST

data value that immediately precedes the data at v in order. Predecessor of a node v in a BST is the node that holds the

#### Finding predecessor

- v has a left subtree
- then predecessor must be the largest value in the left subtree (the rightmost node in the left subtree)
- v does not have a left subtree
- predecessor is the first node on path back to root that does not have v in its left subtree

### Successor in BST

Successor of a node v in a BST is the node that holds the data value that immediately follows the data at v in order.

Finding Successor

- v has right subtree
- successor is smallest value in right subtree (the leftmost node in the right subtree)
- v does not have right subtree
- successor is first node on path back to root that does not have v in its right subtree

### The remove Operation

const () ( دی ٭ if ((t->left != NULL) && (t->right != NULL)) // item not found, do nothing remove(const Comparable& x, BinaryNode<Comparable> t->element = (findMin (t->right)) ->element; t = (t->left != NULL) ? t->left : t->right; BinaryNode<Comparable> \*oldNode = t; remove (t->element, t->right); void BinarySearchTree<Comparable>:: remove(x, t->right); template <class Comparable> remove(x, t->left); if (t->element < x) delete oldNode; if (x < t->element)(t == NULL)return; else { else else Ч - Н

•	peration	
(		
-	Insert (	
•	11	

const insert(const Comparable& x, BinaryNode<Comparable> \*&t // calls private insert( t = new BinaryNode<Comparable>(x, NULL, NULL); // public insert( ) void BinarySearchTree<Comparable>:: void BinarySearchTree<Comparable>:: insert (x, t->left); insert(const Comparable& x) template <class Comparable> template <class Comparable> else if (x < t->element) if (t->element < x) insert (x, root); if (t == NULL) else

; // Duplicate; do nothing

insert (x, t->right);

else

## Implementation of makeEmpty

```
// calls private makeEmpty
                                                                                                                                                                                                                                                                                                    // post order traversal
                                                   // public makeEmpty ()
                                                                                                                                                                                                                                                t) const
                                                                                                                                                                                                                                               makeEmpty(BinaryNode<Comparable> *&
                         void BinarySearchTree<Comparable>::
                                                                                                                                                                                                                    void BinarySearchTree<Comparable>::
                                                                                                                                                                                                                                                                                                                                                        (t->right);
                                                                                                                                                                                                                                                                                                                           makeEmpty (t->left);
template <class Comparable>
                                                                                                                                                                                         template <class Comparable>
                                                                                                                                                                                                                                                                                                if (t != NULL) {
                                                                                                           makeEmpty(root);
                                                                                                                                                                                                                                                                                                                                                       makeEmpty
                                                                                                                                                                                                                                                                                                                                                                                    delete t;
                                                                                                                                                                                                                                                                                                                                                                                                                                        = NULL;
                                                       makeEmpty()
                                                                                                                                                                                                                                                                                                                                                                                                                                          Ļ
```

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#### Tree Iterators

Could provide separate iterators for each desired order

- Iterator<T> \*GetInorderIterator();
- Iterator<T> \*GetPreorderIterator(); I
- Iterator<T> \*GetPostorderIterator (); I
- Iterator<T> \*GetLevelorderIterator (); I

#### Approach 1: Store traversal in list (private data member). Return iterator for list. Tree Iterator Implementation

```
Bnode<T> *node)
Iterator<T> BinaryTree::GetInorderIterator()
                                                                           FullListInorder(m theList, getRoot());
                                                                                                                                                                                                                                  FillListInorder(ArrayList<T> *lst,
                                                                                                            return m_theList->GetIterator();
                                     m theList = new ArrayList<T>;
                                                                                                                                                                                                                                 void
```

```
FillListInorder(lst, node->right);
                                    FillListInorder(lst, node->left);
if (node == NULL) return;
                                                                             lst->Append(node->data);
```

### Tree Iterators (cont)

### Approach 2: store traversal in stack to mimic recursive traversal

```
template <class T>
class InOrderIterator
{
    private:
```

Stack<\* BNode<T> > m stack;

```
{return !m_stack.isEmpty(); }
                                                bool hasNext() // aka isPastEnd
                        InOrderIterator(BinaryTree<T> *t);
                                                                                                   // aka advance()
                                                                                                      T Next();
public:
```

### Tree Iterators (cont'd)

// and all left descendants InOrderIterator<T>::InOrderIterator(BinaryTree<T> \*t) // push root BNode<T> \*v = t-setRoot(); m\_stack.Push(v); while (v != NULL) { v = v -> left;template <class T>

### Tree Iterators (cont'd)

```
// and all left descendants
                                                                                                                                                                                                            // push right child
                                                                                       Bnode<T> *top = m_stack.Top();
                              T InOrderIterator<T>::Next()
                                                                                                                                                  BNode<T> *v = top->right;
                                                                                                                                                                                                                                                                                                      return top->element;
                                                                                                                                                                                                           m_stack.Push(v);
                                                                                                                                                                             while (v != NULL) {
                                                                                                                                                                                                                                           v = v - > left;
template <class T>
                                                                                                                    m_stack.Pop();
```