CMSC 341 Data Structures

Red-Black Tree Review

These questions will help test your understanding of the Red-Black tree material discussed in class and in the text. These questions are only a study guide. Questions found here may be on your exam, although perhaps in a different format. Questions NOT found here may also be on your exam. The rotation diagrams for red-black trees *may* be provided with your exam. Check with your instructor.

- 1. Define *Red-Black tree*. List all Red-Black tree properties
- 2. Define the *black height* of a node, *x*.
- 3. What is the "Big-Oh" performance (in terms of the number of nodes in the tree) for the operations **find**, **insert** and **remove** for a red-black tree in the best, worst and averages cases?
- 4. What property of red-black trees is most significant in explaining the "Big-Oh" performance for the operations **find, insert** and **remove**?
- 5. Prove that in any red-black tree with root x, there are at least $n = 2^{bh(x)} 1$ internal nodes where bh(x) is the black-height of x.
- 6. Prove that in any red-black tree, at least half the nodes on any path from the root to a leaf must be black.
- 7. Prove that in any red-black tree, no path from any node, N, to a leaf is more than twice as long as any other path from N to any other leaf.
- 8. Prove that if a black node has just one child, that child must be red.
- 9. Show the tree that results from inserting the values **2**, **1**, **4**, **5**, **9**, **3**, **6**, **7** into an initially empty red-black tree. Show the tree after each insertion.

10. Given the following Red-Black Tree, show the tree that results after deleting the node with value **40** using bottom-up deletion.





